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# Model-based methods to improve computing times in linear energy system optimization models

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DLR – German Aerospace Center, Department of Energy Systems Analysis

a project by



Deutsches Zentrum  
für Luft- und Raumfahrt  
German Aerospace Center

- Motivation
- Repetition: *Characteristics and dimensions of Energy system optimization models*
- Theory: *Classification of existing approaches*
- Evaluation methodology
- Results and major findings
- Conclusions

# Motivation

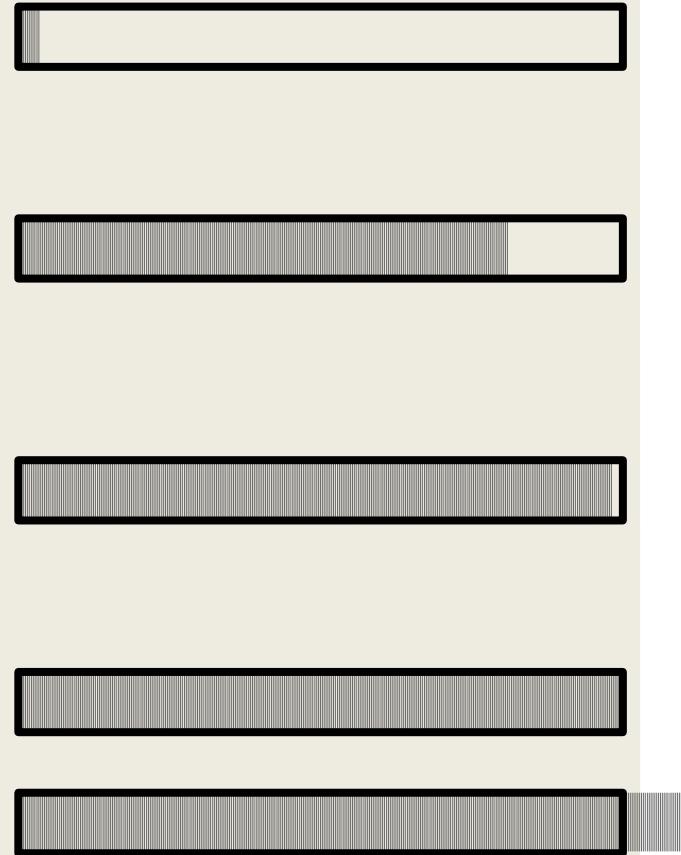
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## What can modelers do?

What have modelers  
done  
themselves?

Project starts

Time budget

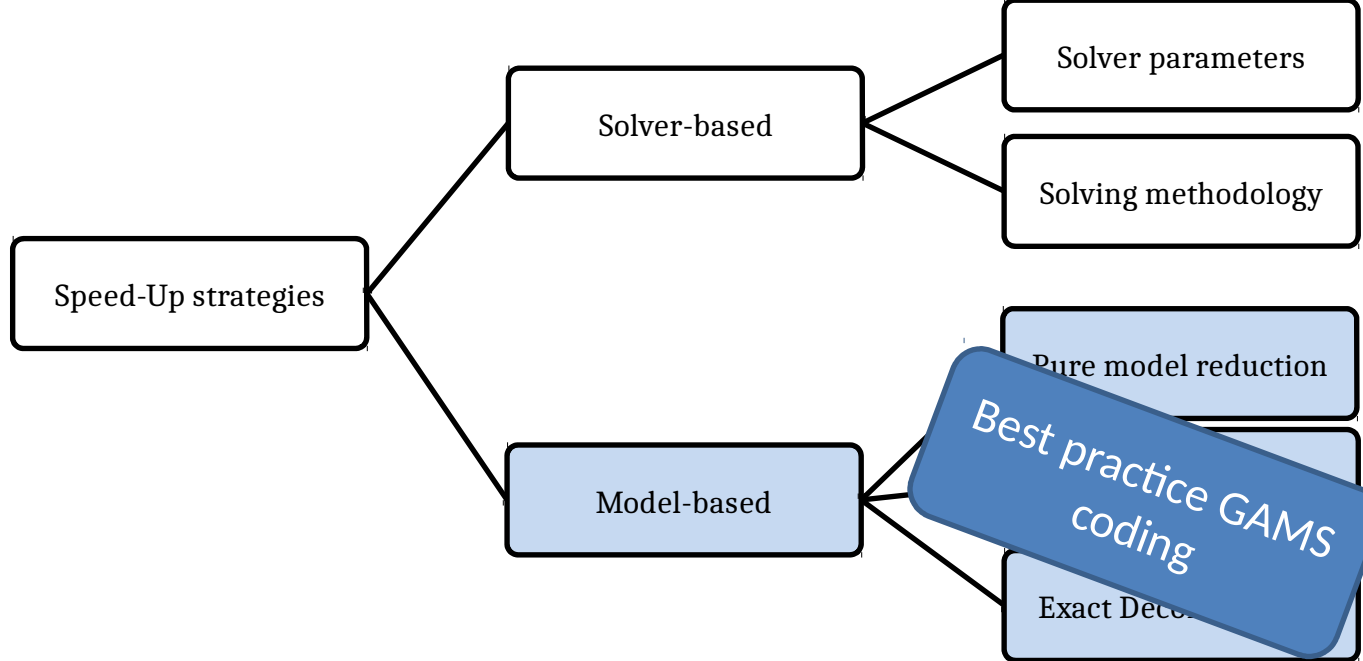


Which **speed-up** is possible  
using measures that can be  
influenced by „normal“ model  
developers?

- Large applied Energy System Optimization Models
  - LPs
  - Computing time: >12h (dominated by solver)
  - Storage and transmission
- Shared memory hardware
- Use of standard solvers



# Basic approaches (try that first)



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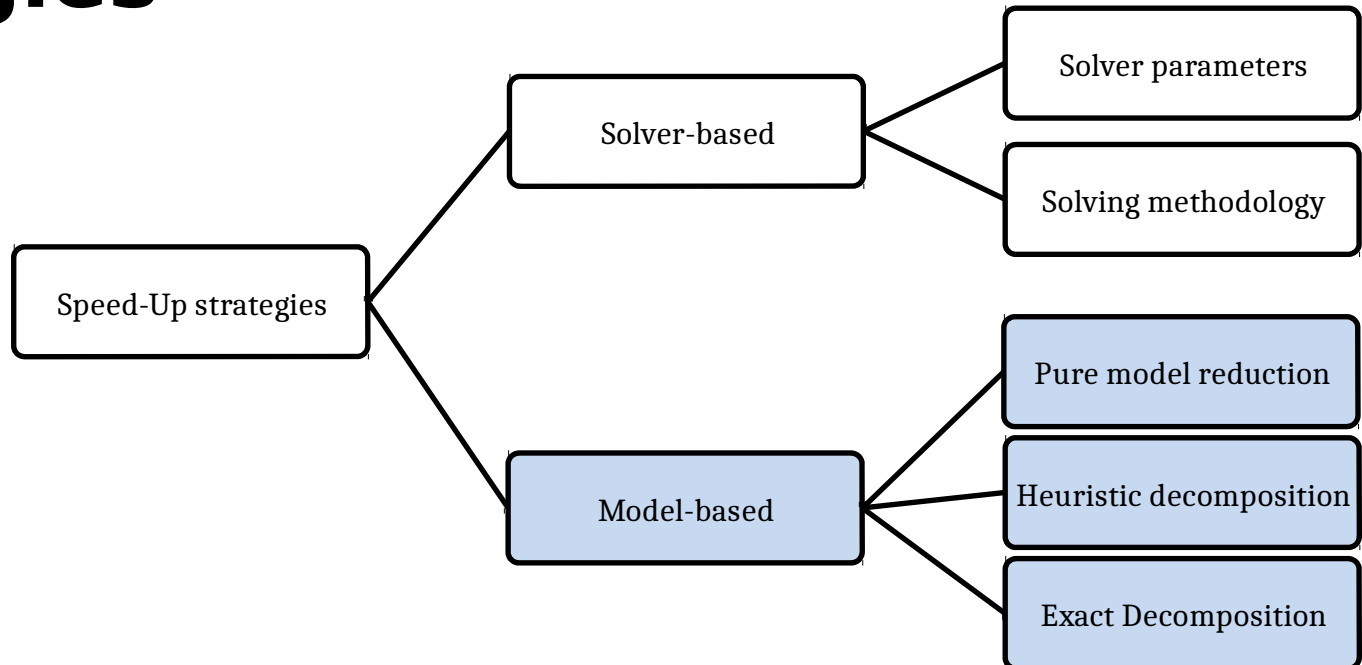


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- **Selection of measures (also useful for decrease memory need):**
  - Input data should not differ much in its order of magnitude
  - Index order influences computing time
    - Useful, but not necessarily faster
    - Assignment statements with a different set order can be faster
    - It can be better to place large index sets at the beginning
  - Use of “option kill” , e.g. for long time-series input parameters saves memory
  - Abundant use of “Dollar Control over the Domain of Definition”
  - Consistent (and limited) use of defined variables
  - Avoidance of the consideration of technologies providing the same service at the same costs
  - Consideration of alternative formulation of model constraints (dense vs. sparse)
- **Helpful references:** “Speeding up GAMS Execution Time” by Bruce A. McCarl <https://www.gams.com/mccarl/speed.pdf>

# Approach II: Model-based speed-up strategies

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# Typical model dimensions

## Time

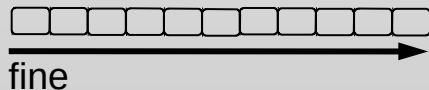
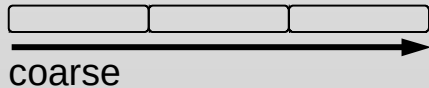
Planning horizon

Operation

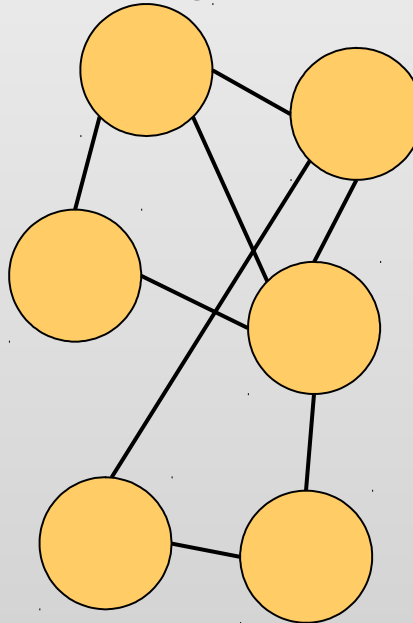
Investment

Short term Long term

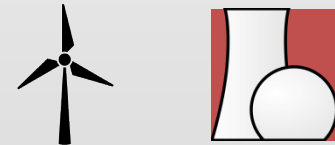
Discretisation



## Regions



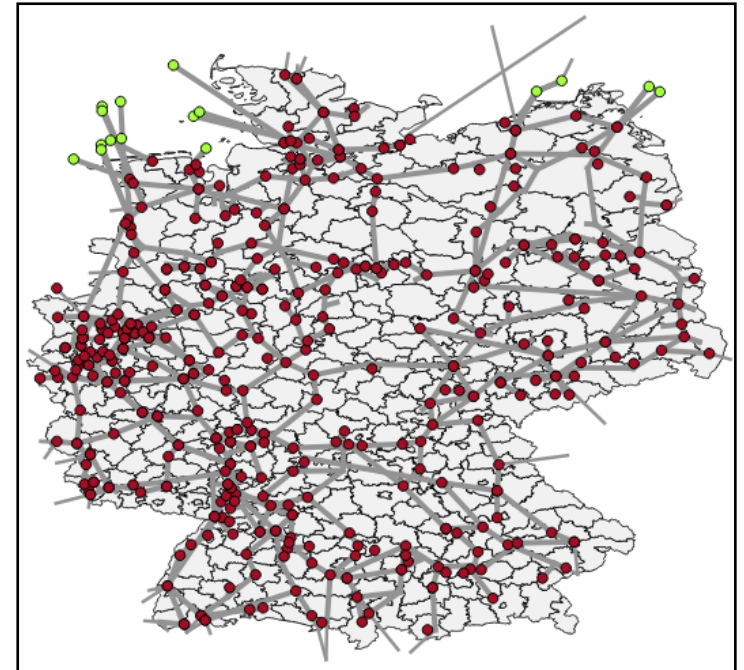
## Technology



# **Characteristics and dimensions of Energy system optimization models**

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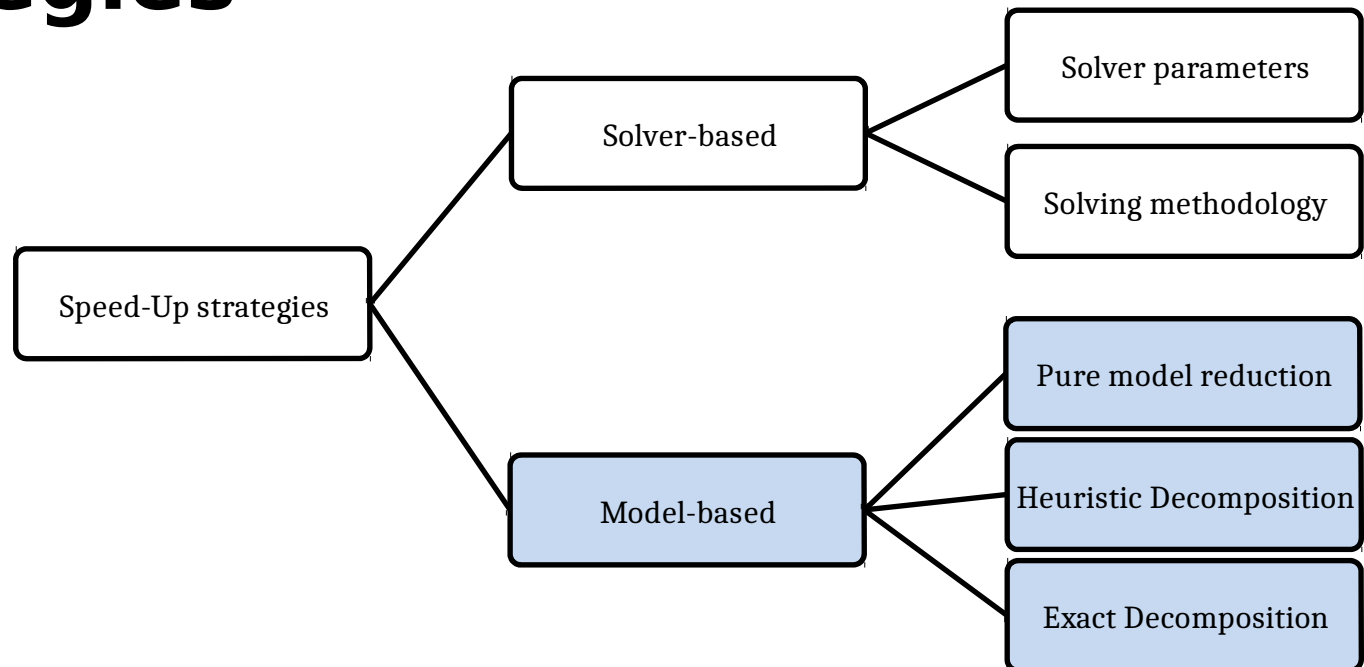
Model name	REMix
Author (Institution)	German Aerospace Center (DLR)
Model type	Linear programming minimization of total costs for system operation <b>economic dispatch</b> / optimal dc power flow with <b>expansion of storage and transmission capacities</b>
Sectoral focus	Electricity
Geographical focus	Germany
Spatial resolution	> 450 nodes (reference model)
Analyzed year (scenario)	2030
Temporal resolution	8760 time steps (hourly)



Solver	Commercial
Algorithm	Barrier
Cross-over	Disabled
Max. parallel barrier threads	16
Scaling	Aggressive

# Model-based speed-up strategies

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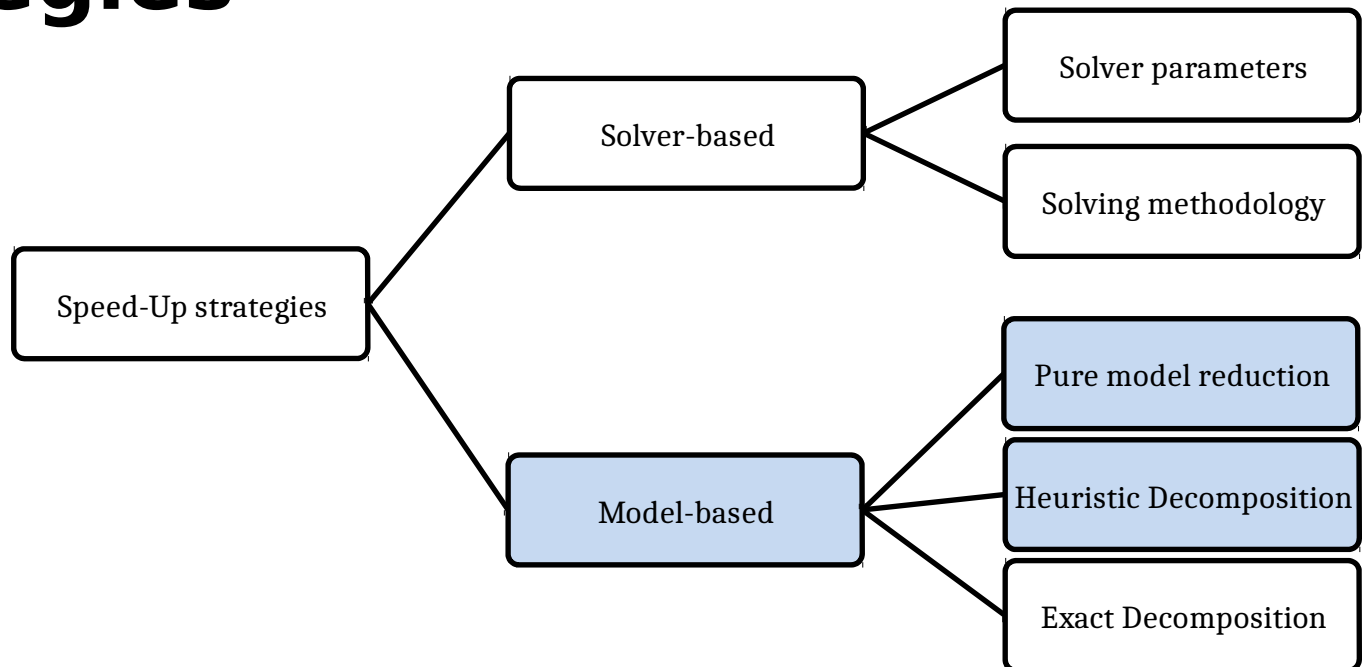
# Literature Review

Authors	Math. problem type	Descriptive problem type	Decomposed model scale	Decomposition technique
Alguacil and Conejo [56]	MIP/NLP	Plant and grid operation	Time, single sub-problem	Benders decomposition
Amjady and Ansari [57]	MIP/NLP	Plant operation		Benders decomposition
Binato et. al [58]	MIP/LP	TEP		Benders decomposition
Esmaili et. al [59]	NLP/LP	Grid operation		Benders decomposition
Flores-Quiroz et. al [60]	MIP/LP	GEP	Time, 1-31 sub-problems, sequentially solved	Dantzig-Wolfe decomposition
Habibollahzadeh et. al [61]	MIP/LP	Plant operation		Benders decomposition
Khodaei et. al [62]	MIP/LP	GEP-TEP	Time, 2 sub-problem types, sequentially solved	Benders decomposition
Martinez-Crespo et. al [63]	MIP/NLP	Plant and grid operation	Time, 24 sub-problems, sequentially solved	Benders decomposition
Roh and Shahidehpour [64]	MIP/LP	GEP-TEP	Time, up to 10 • 4 sub-problems, sequentially solved	Benders decomposition and Lagrangian Relaxation
Virmani et. al [65]	LP/MIP	Plant operation	Technology (generation units), up to 20 sub-problems, sequentially solved	Lagrangian Relaxation
Wang et. al [66]	LP/MIP	Plant and grid operation	Space, 26 sub-problems, sequentially solved	Lagrangian Relaxation
Wang et. al [67]	MIP/NLP	Plant and grid operation	Scenarios and time, 10 • 4 sub-problems, sequentially solved	Benders decomposition
Wang et. al [68]	LP	Plant and grid operation	Technology (circuits) and time (contingencies), 2 sub-problem types, sequentially solved	Lagrangian Relaxation and Benders decomposition

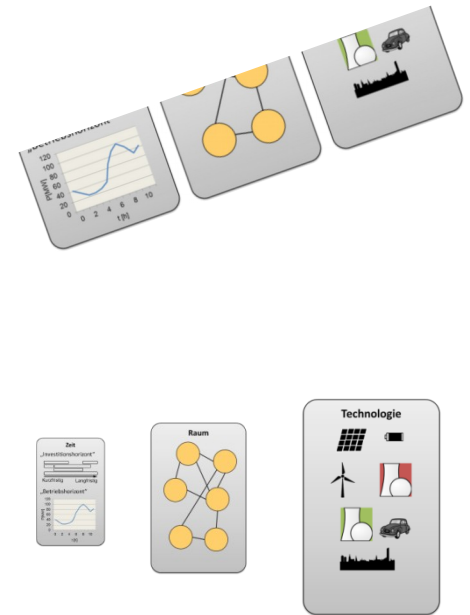
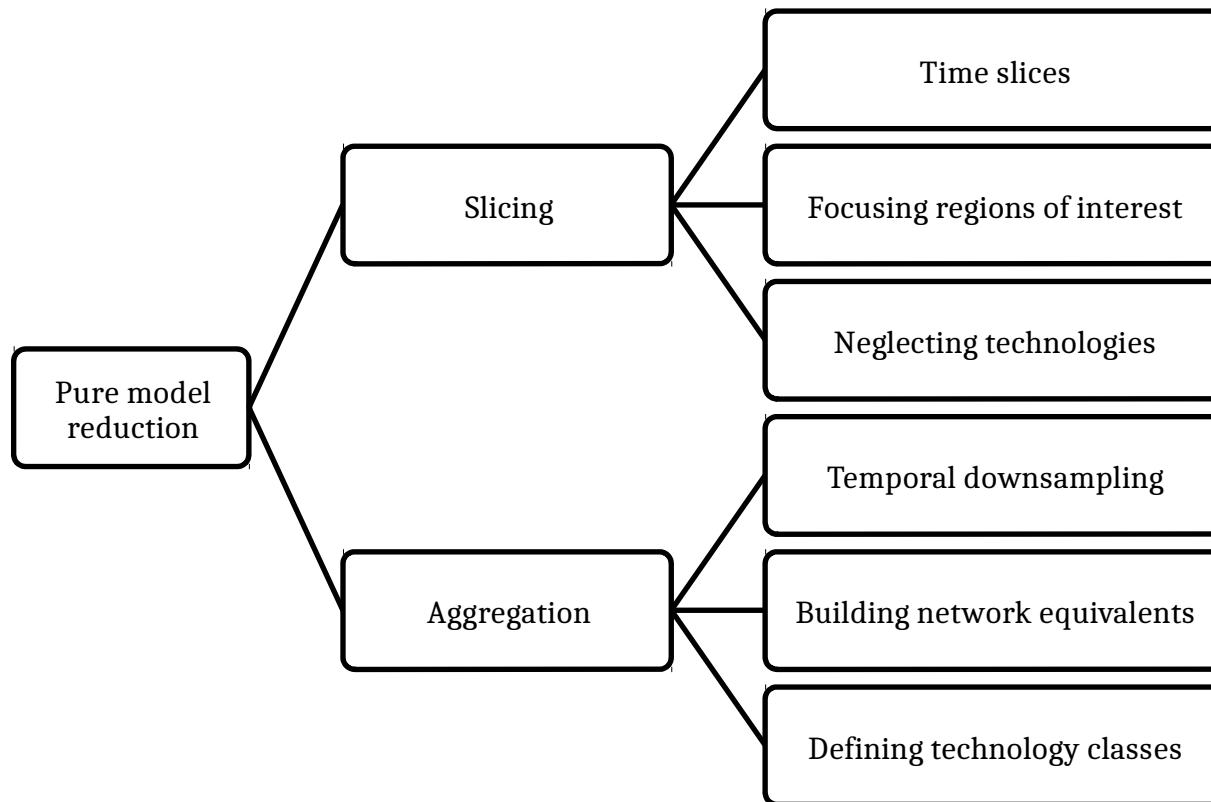


# Model-based speed-up strategies

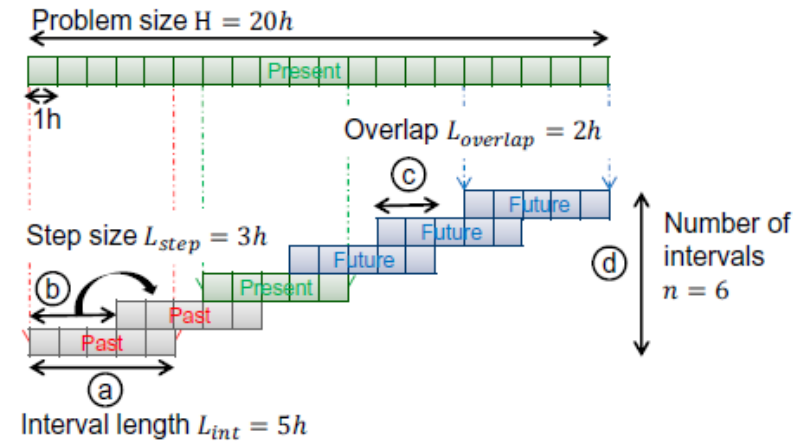
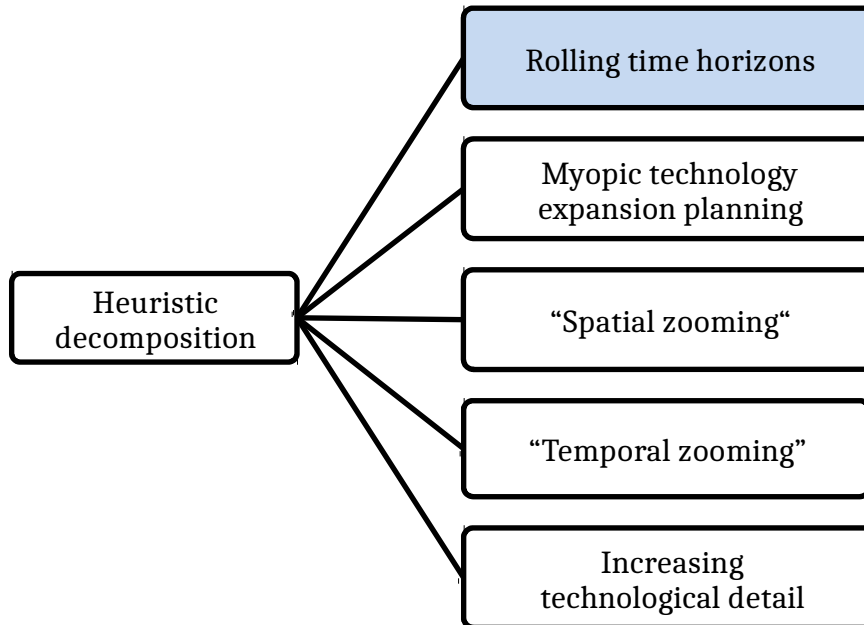
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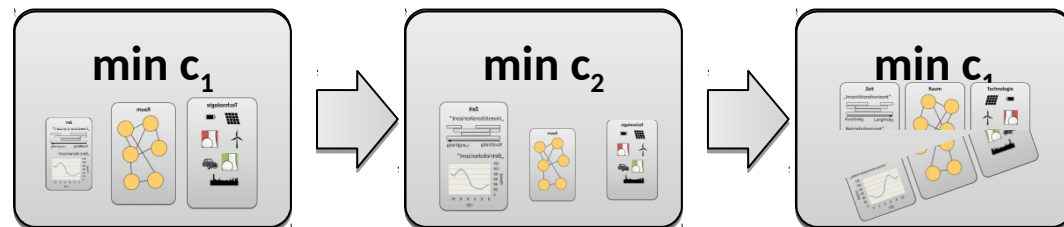
# Types of model reductions in ESM



# Meta heuristics



Stepwise solving  
reduced models



*„Decomposition which is  
**similar**  
to exact decomposition  
approaches  
that are stopped  
within the first iteration“*

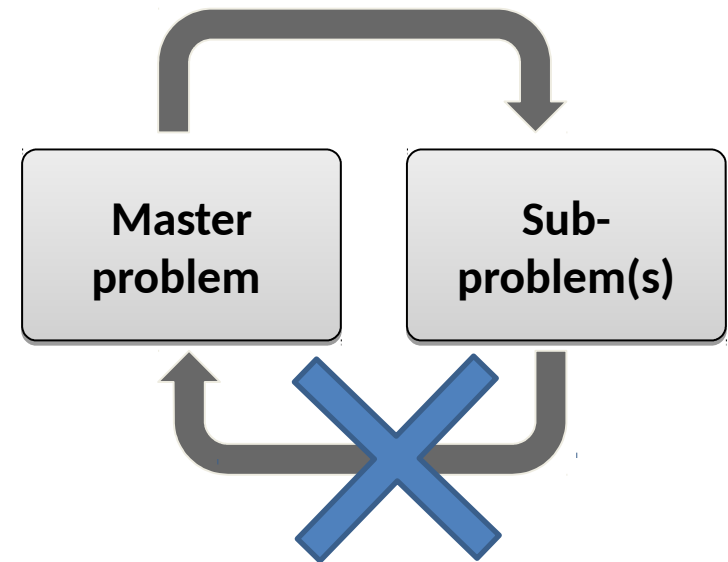
Rolling time horizons

Myopic technology  
expansion planning

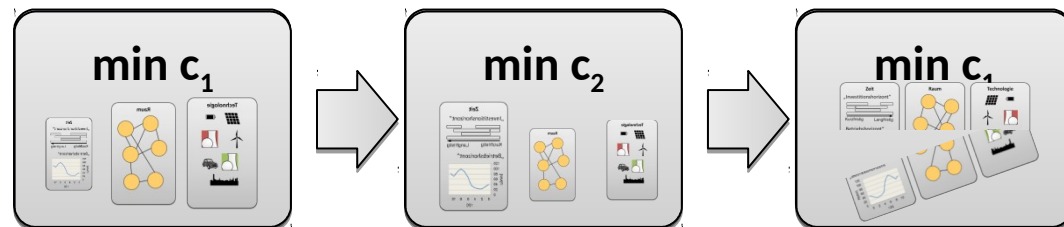
“Spatial zooming”

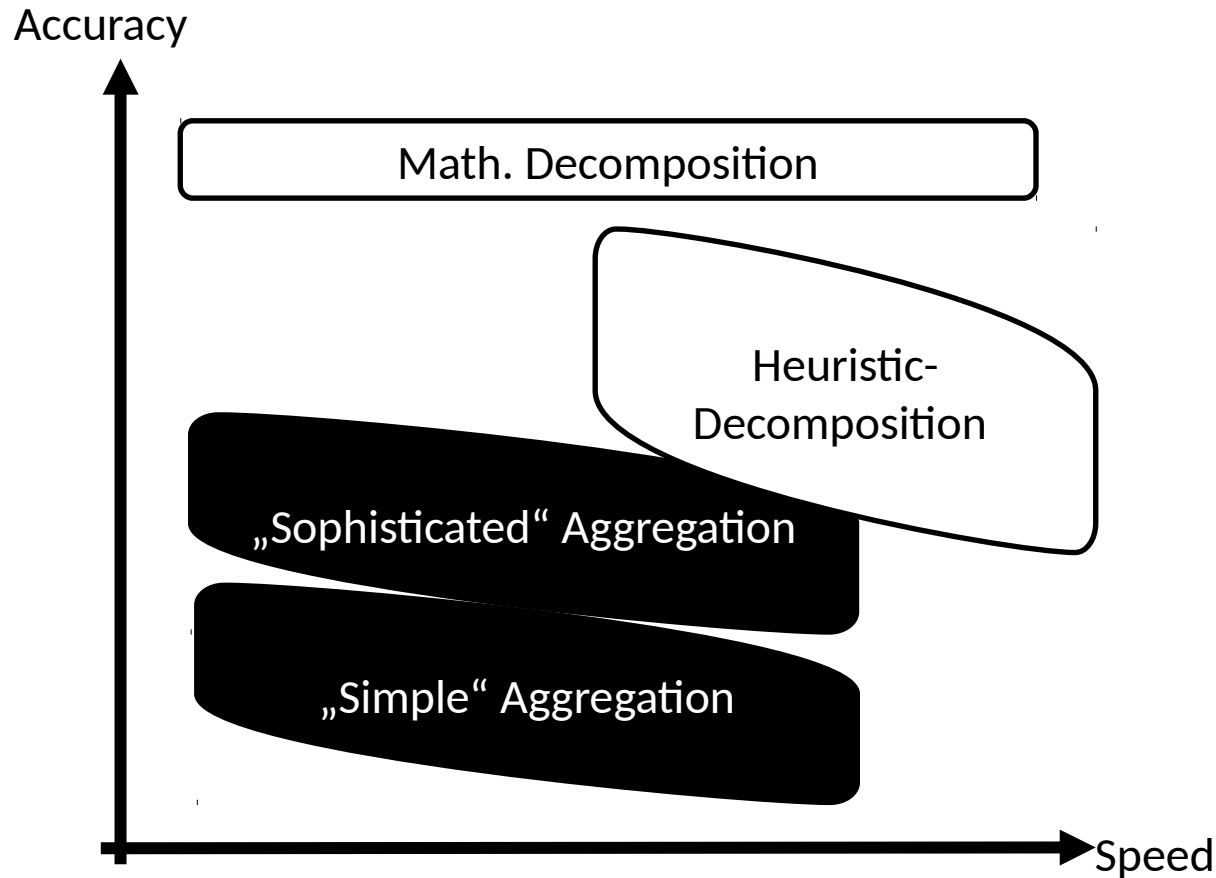
“Temporal zooming”

Increasing  
technological detail



Stepwise solving  
reduced models



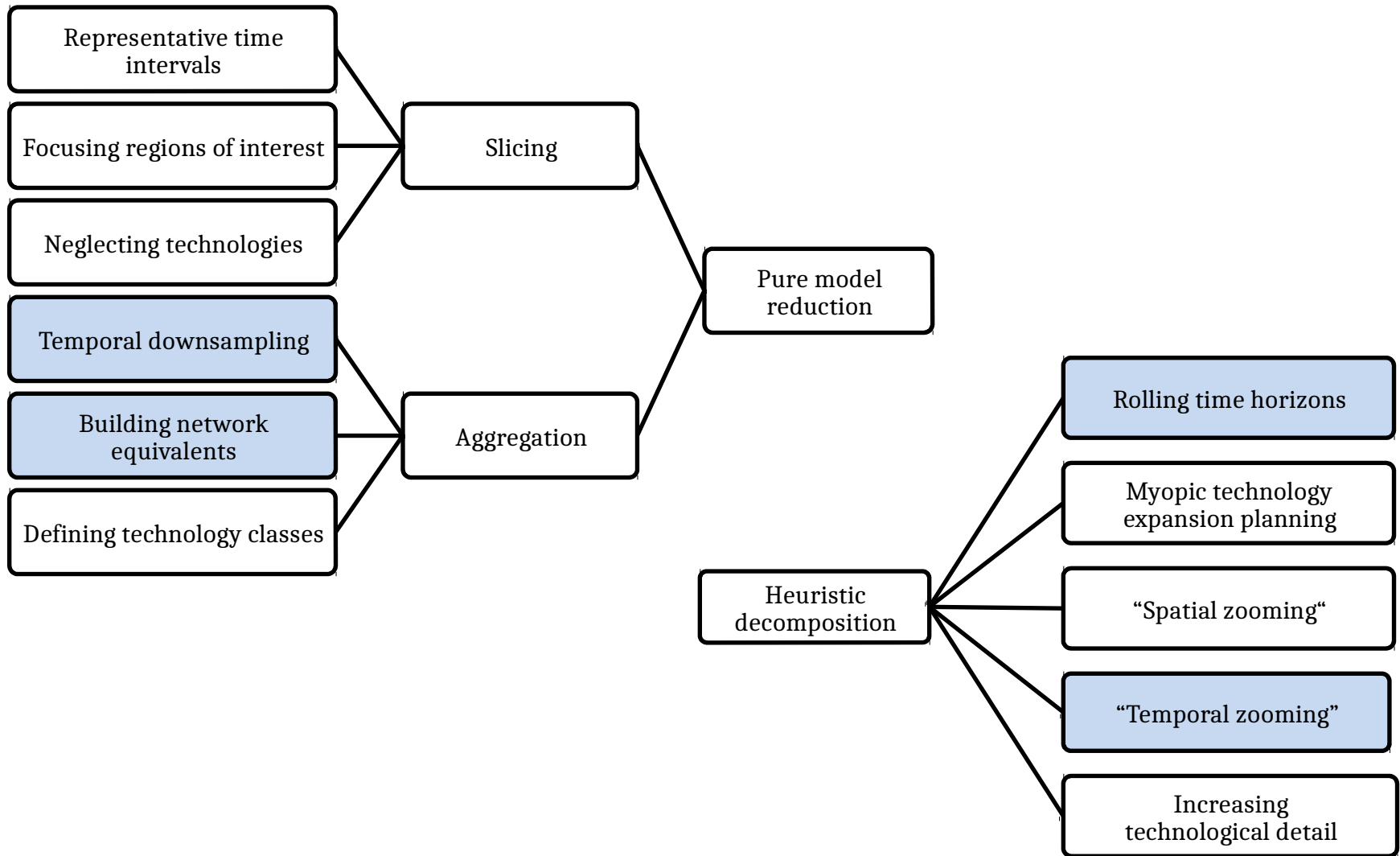


PIPS

# Evaluation methodology

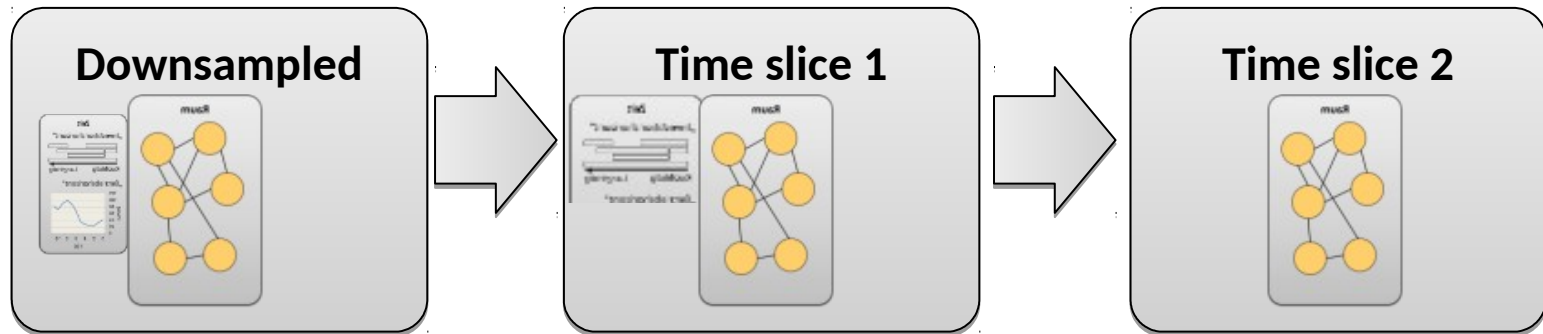
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# Evaluated speed-up

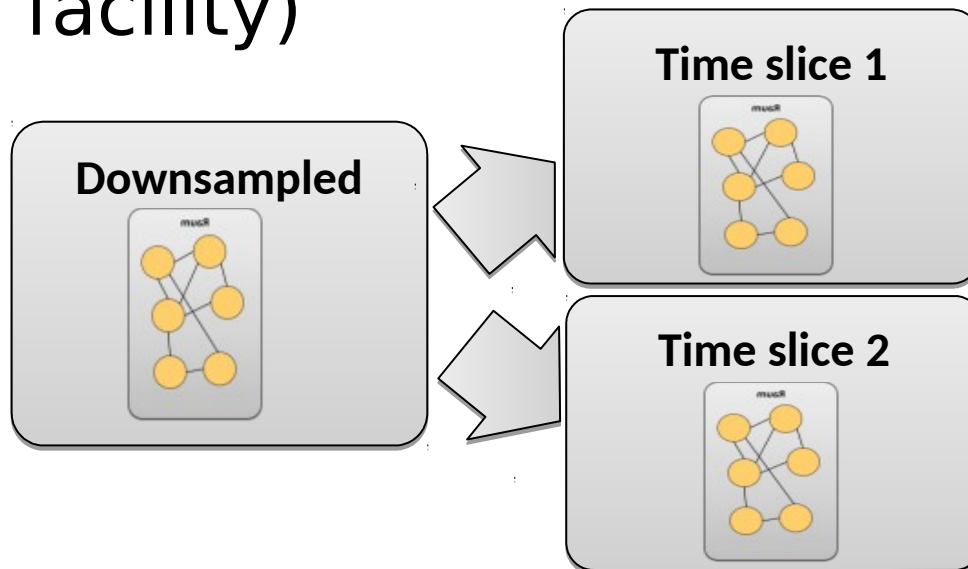


# „Temporal zooming“ implementations

- Sequential



- Parallel (using GAMS's grid computing facility)





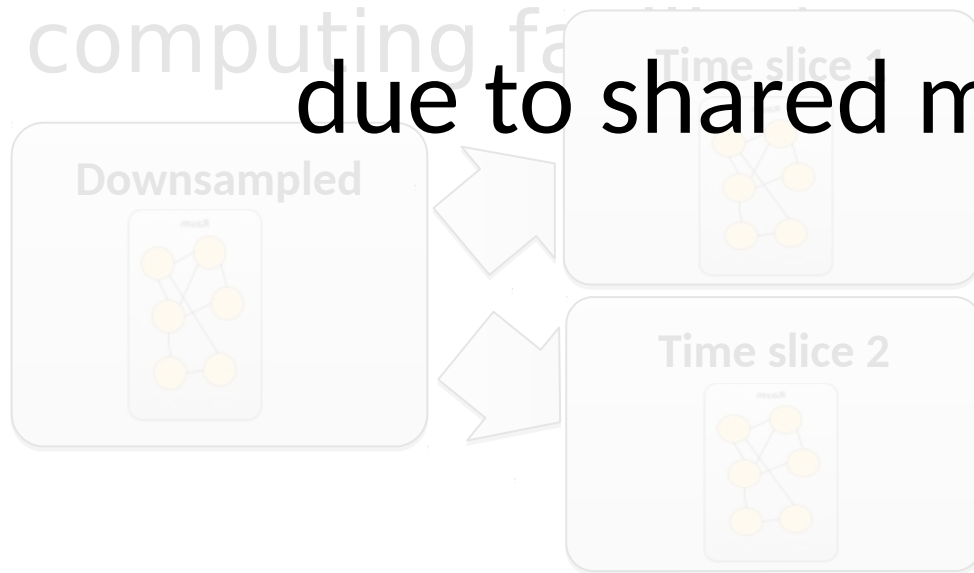
# „Temporal zooming“

- Sequential



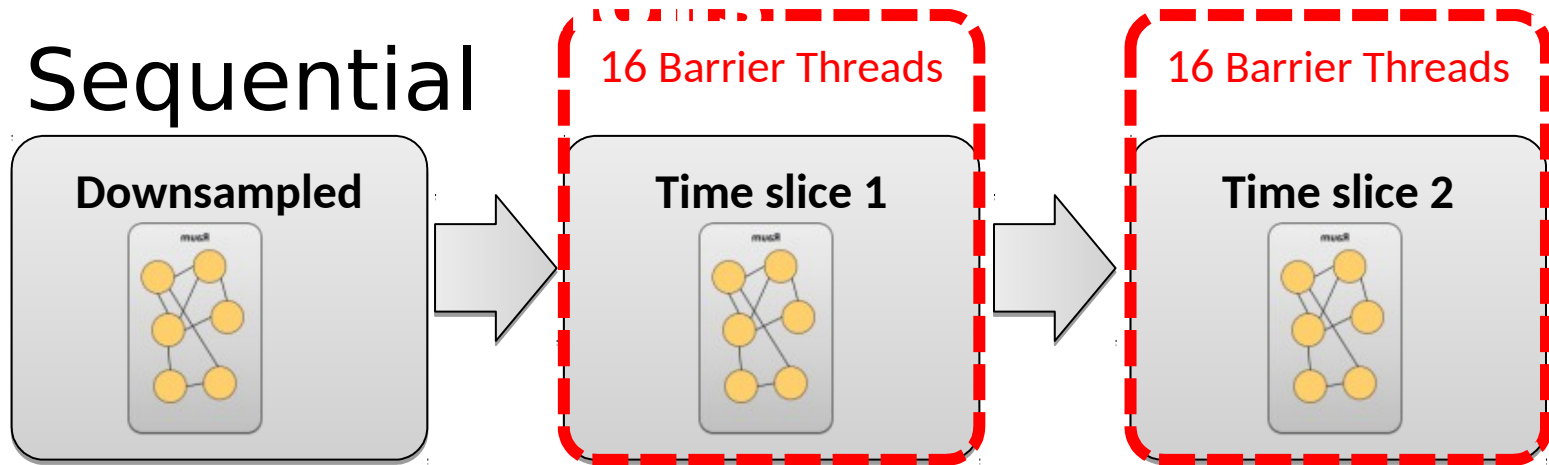
Parallelization limited

- Parallel (using GAMS's grid computing framework)  
due to shared memory!

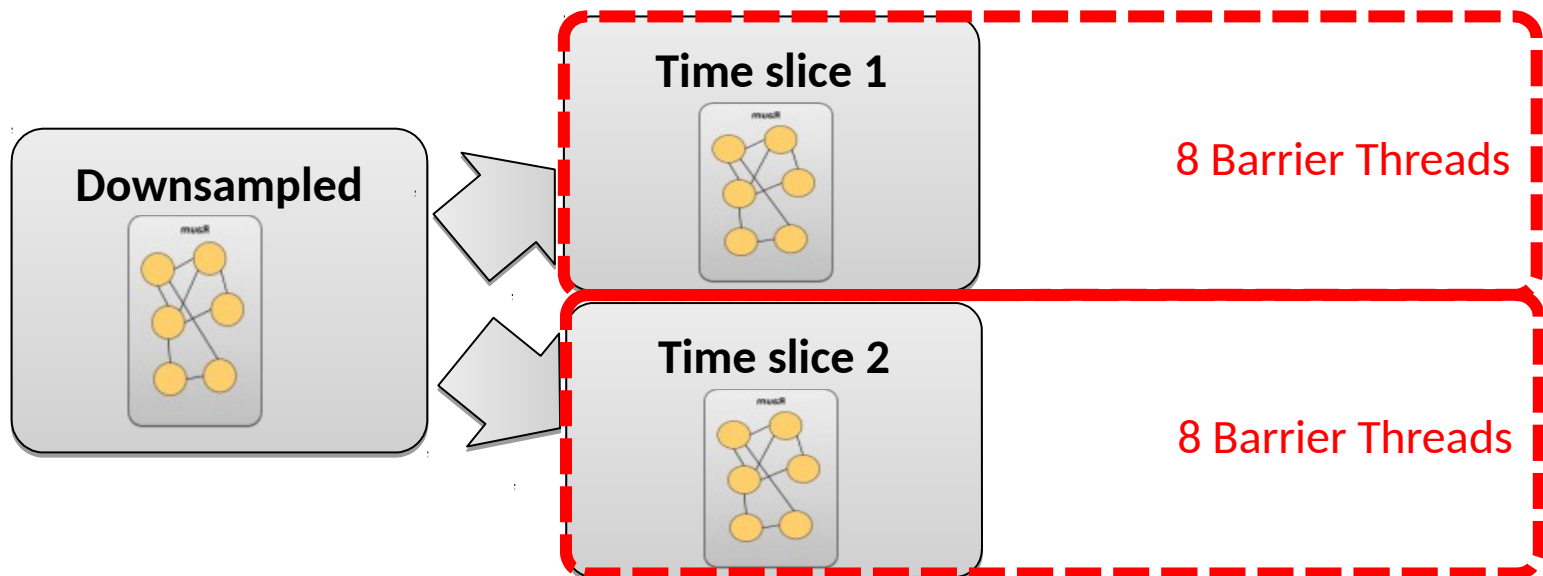


# „Temporal zooming“

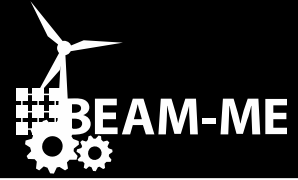
- Sequential



- Parallel (using GAMS's grid computing facility)



# Speed-up approach parameters

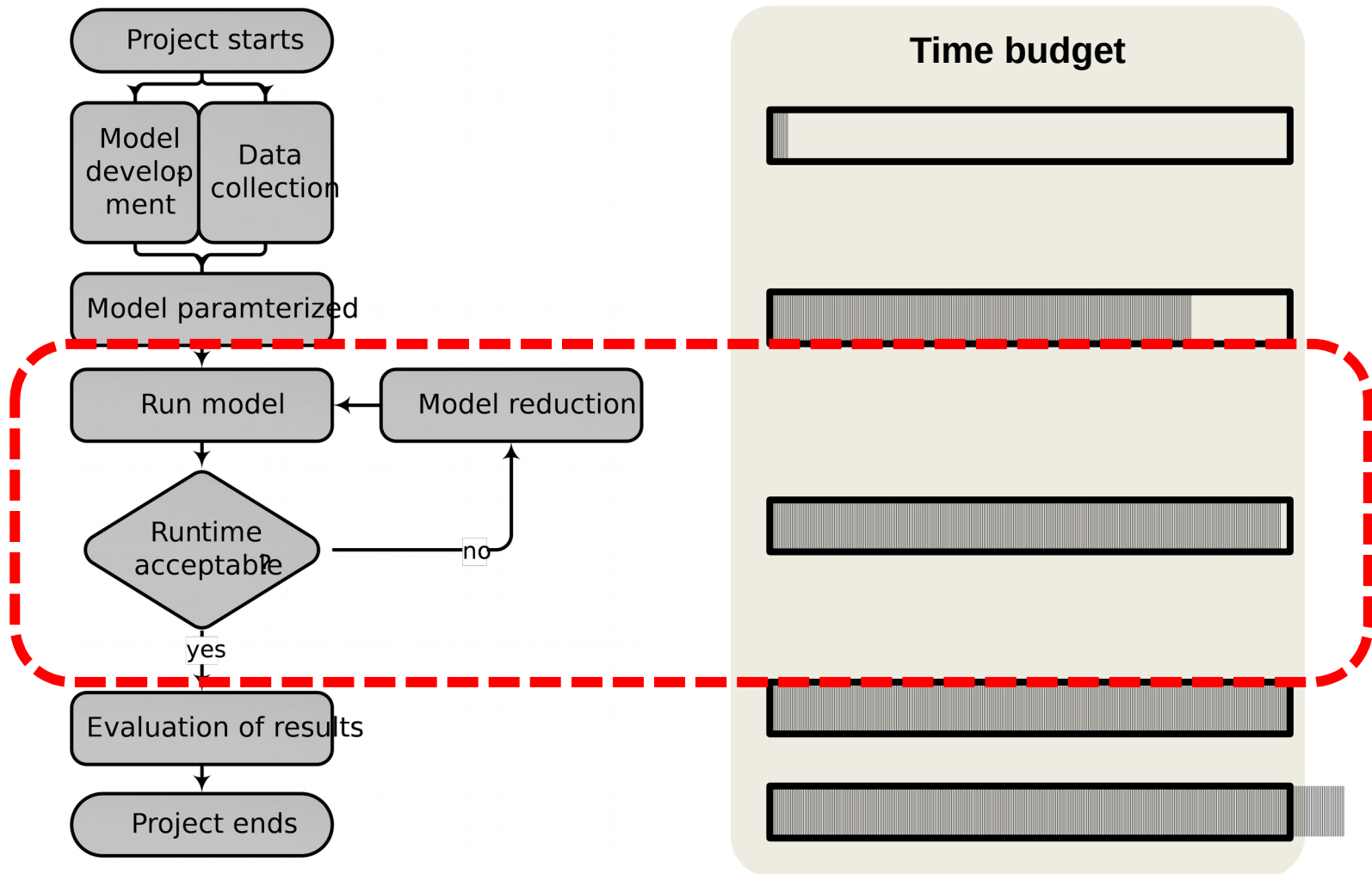


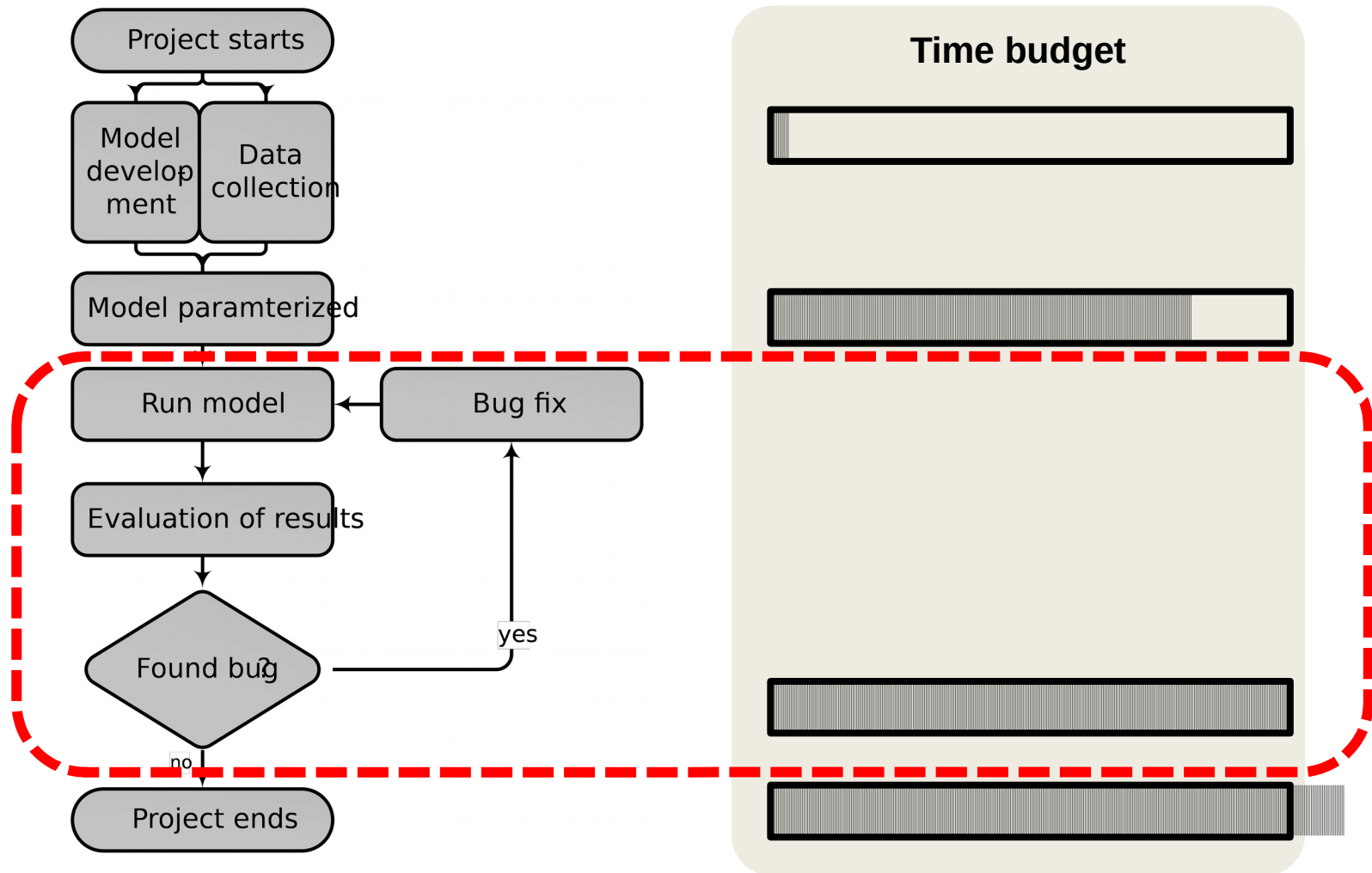
Speed-up approach	w*	wo*	Name	Evaluated range
Spatial aggregation	P	P	number of regions (clusters)	{1, 5, 18, 50, 100, 150, 200, 250, 300, 350, 400, 450, 488}
Temporal Downsampling	P	P	temporal resolution	{1, 2, 3, 4, 6, 8, 12, 24, 48, 168, 1095}
Rolling horizon dispatch	O	P	number of intervals	{4, 16, 52}
			overlap size	{1%, 2%, 4%, 10%}
Temporal zooming (sequential)	P	O	number of intervals	{4, 16, 52}
			resolution of down-sampled run	{4, 8, 24}
Temporal zooming (grid computing)	P	O	number of intervals	{4, 16, 52}
			resolution of down-sampled run	{4, 8, 24}
			number barrier threads	{2, 4, 8, 16}
			number of parallel runs	{2, 4, 8, 16}

\*w/wo: expansion of storage and transmission capacities

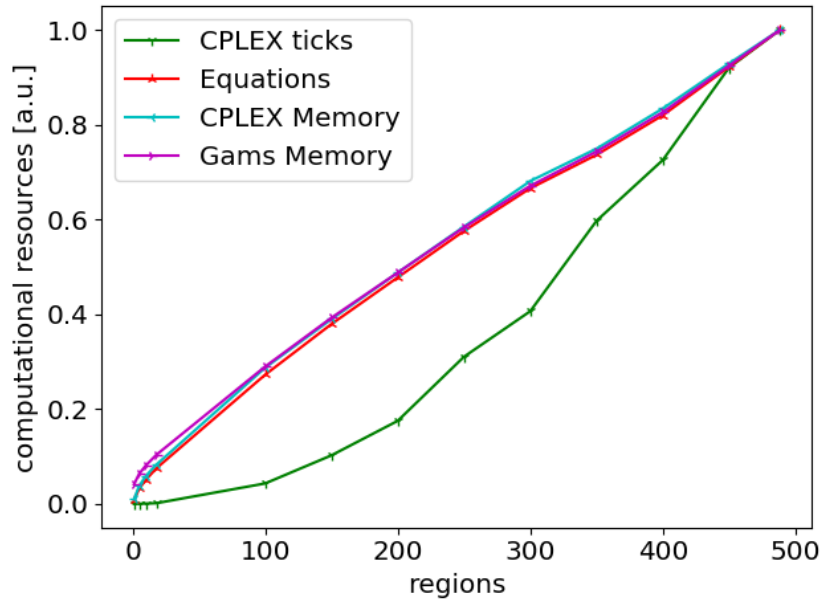
# Results

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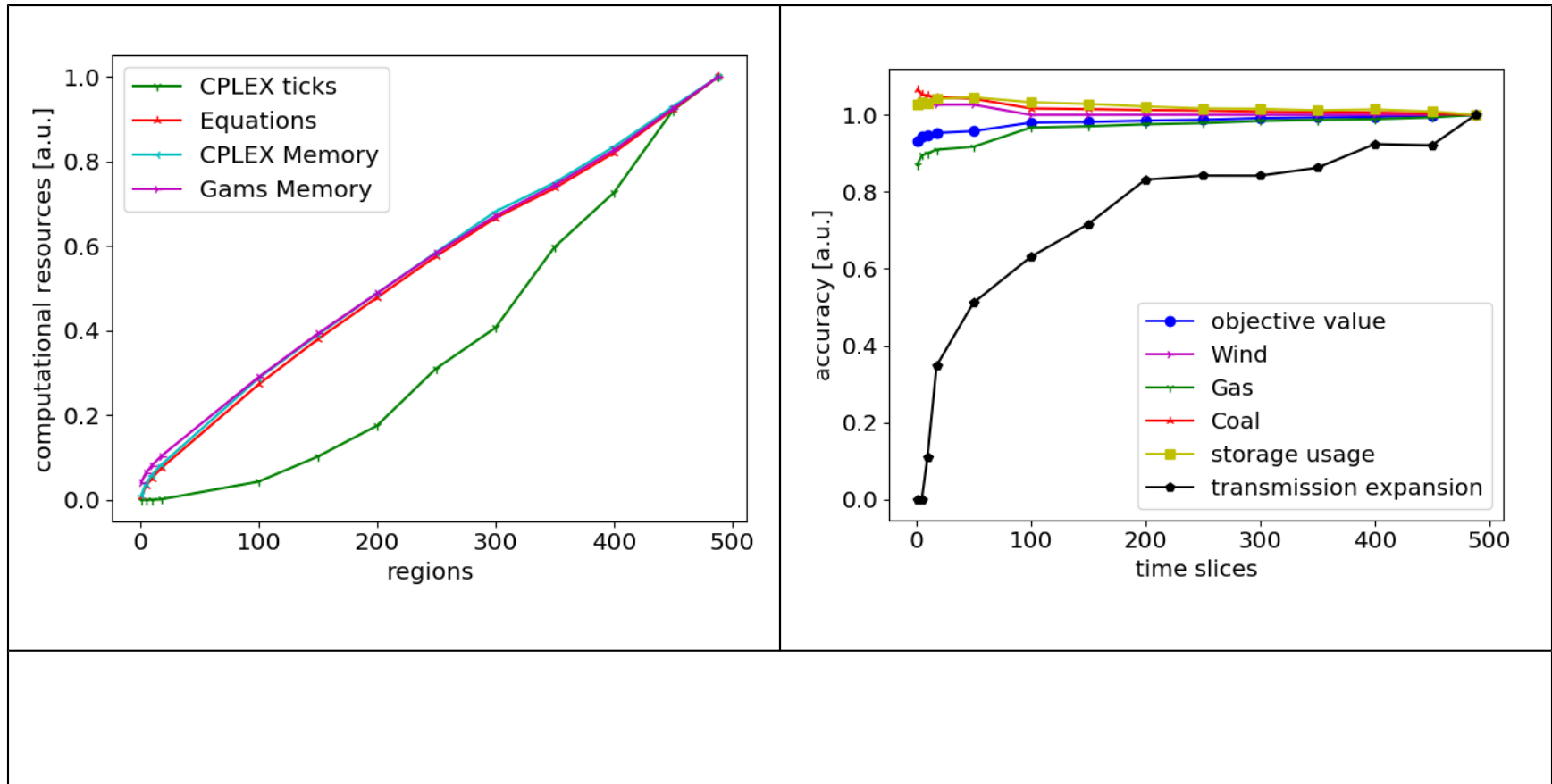




## Performance

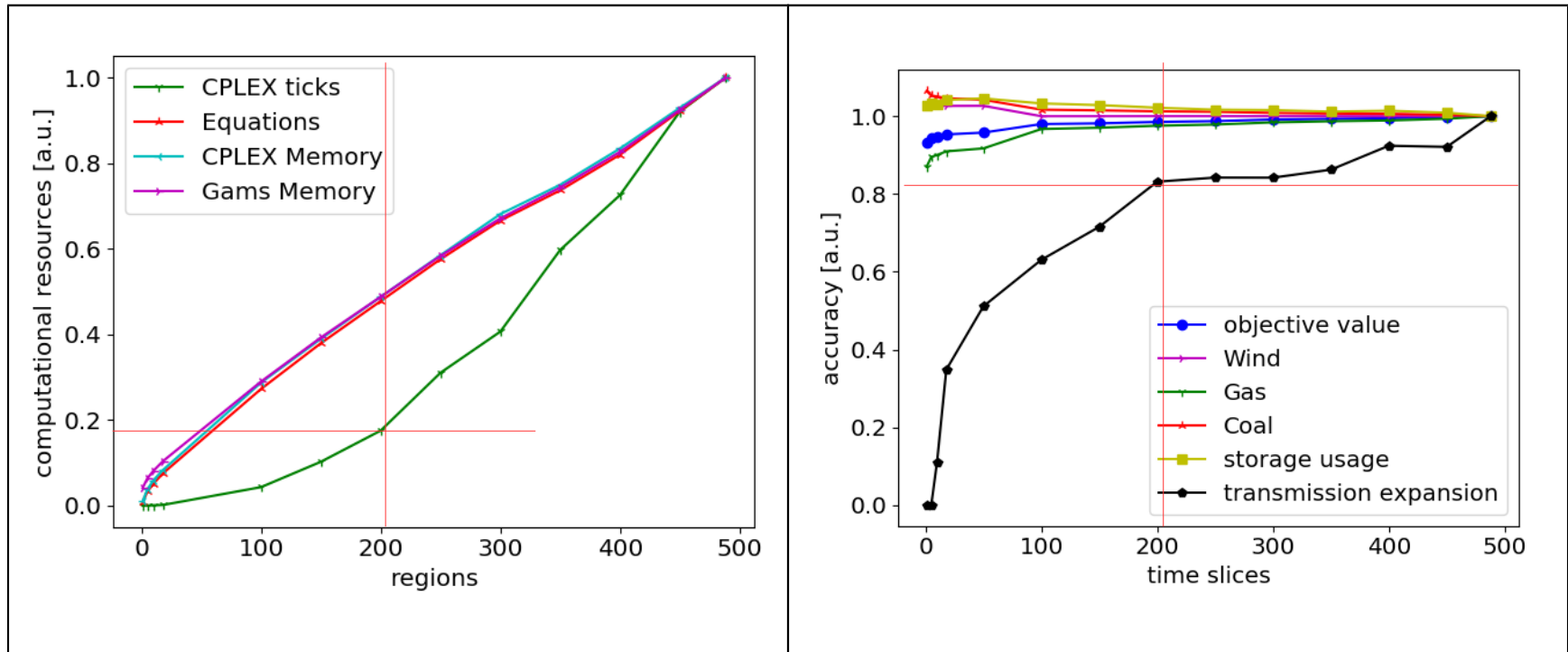


## Performance





## Performance

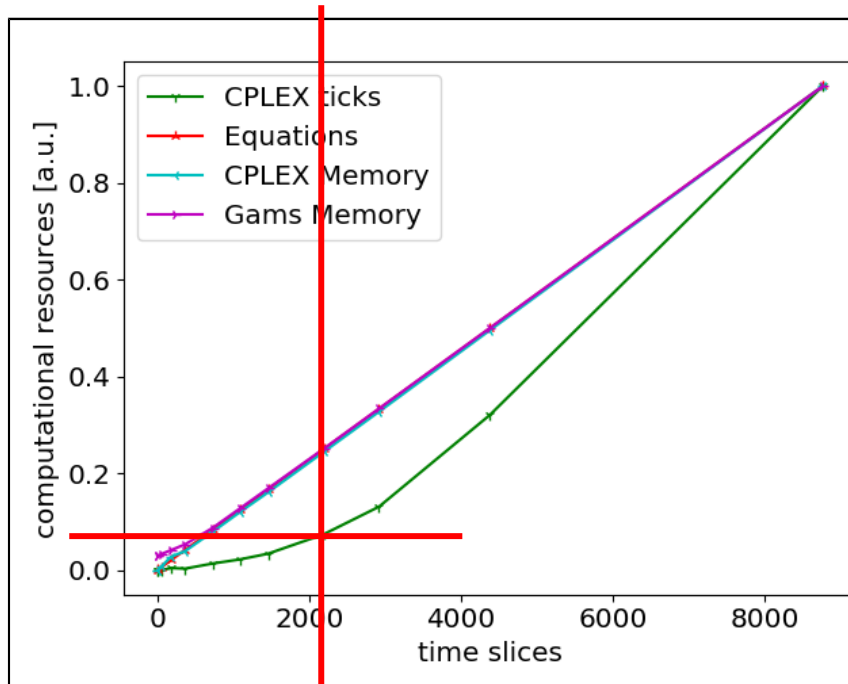


1 a) Speed-up factor:  $\approx 5$

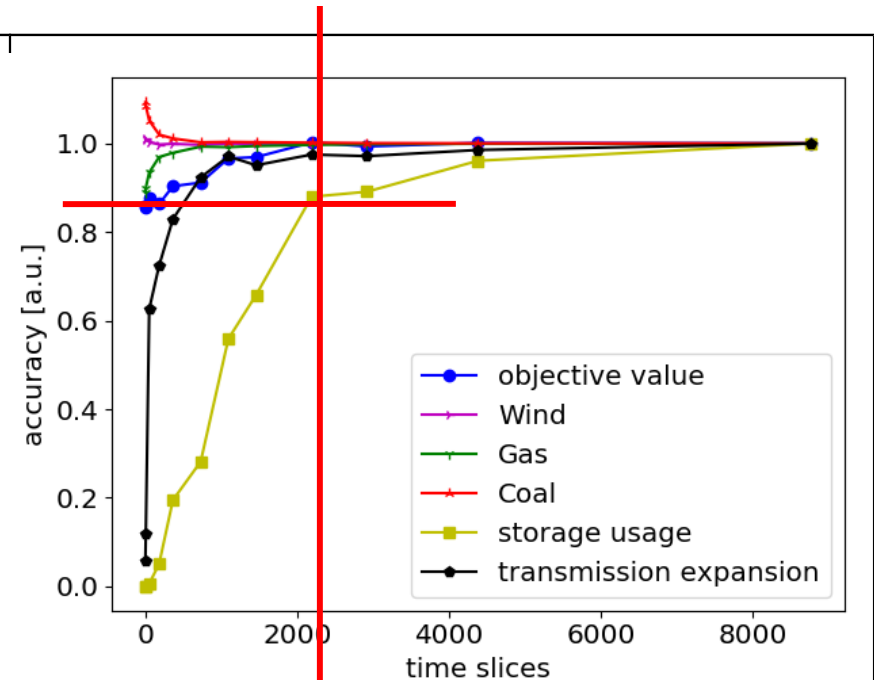
2 a) Accuracy error mainly  $< 10\%$  (grids:  $\approx 20\%$ )

# Temporal downsampling (w exp)

## Performance



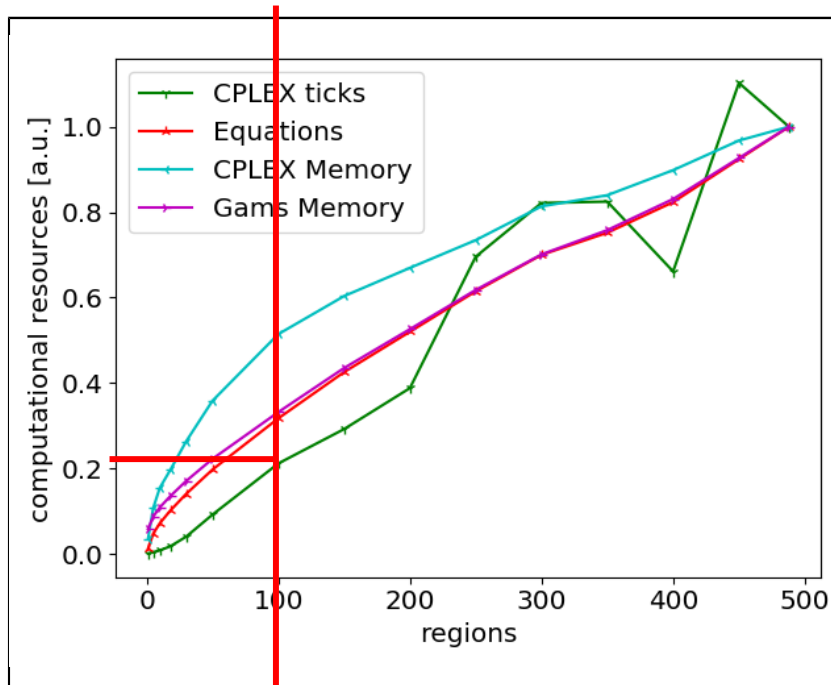
## Accuracy



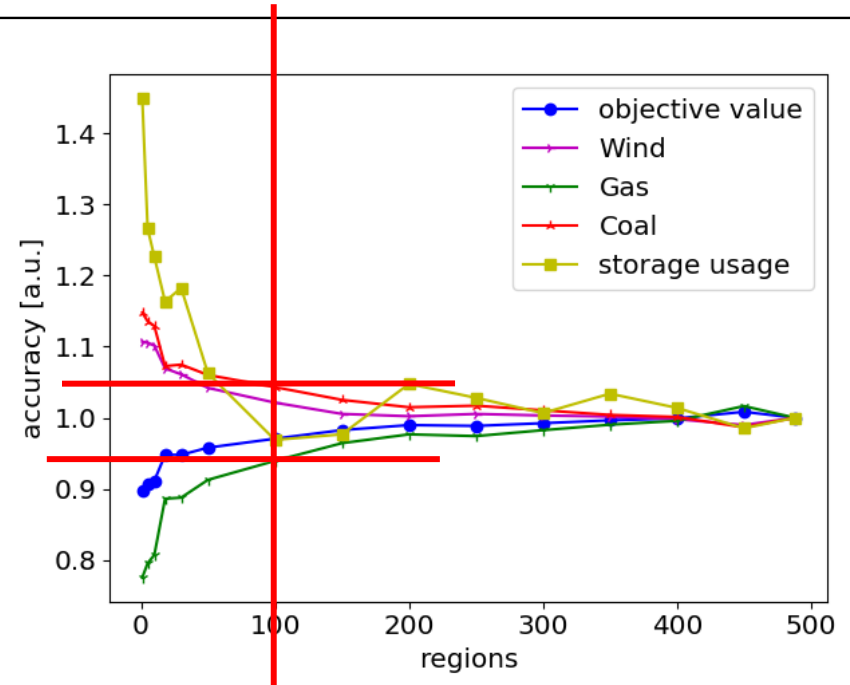
- 1 b) Speed-up factor:  $\approx 10$
- 2 b) Accuracy error mainly  $< 10\%$  (storage:  $\approx 20\%$ )

# Spatial downsampling (wo exp)

## Performance



## Accuracy

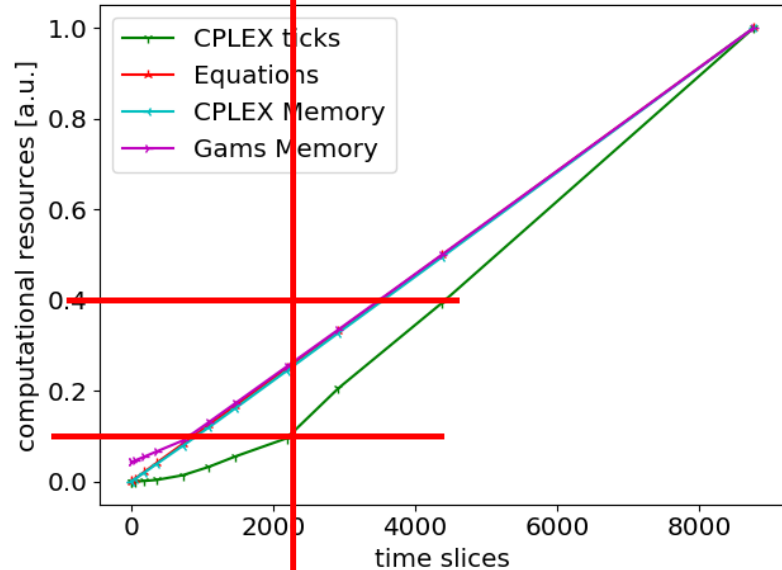


1 b) Speed-up factor:  $\approx 5$

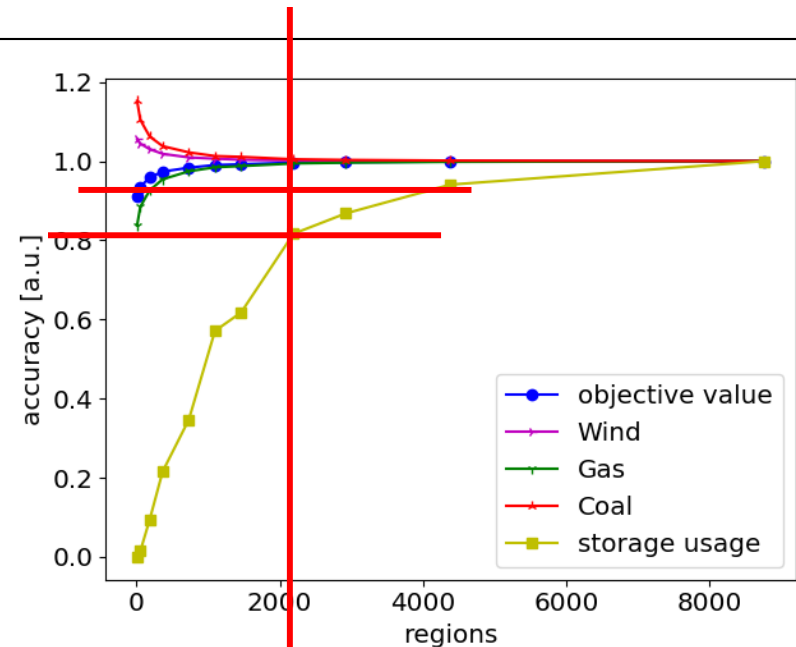
2 b) Accuracy error mainly  $< 10\%$

# Temporal downsampling (wo exp)

## Performance



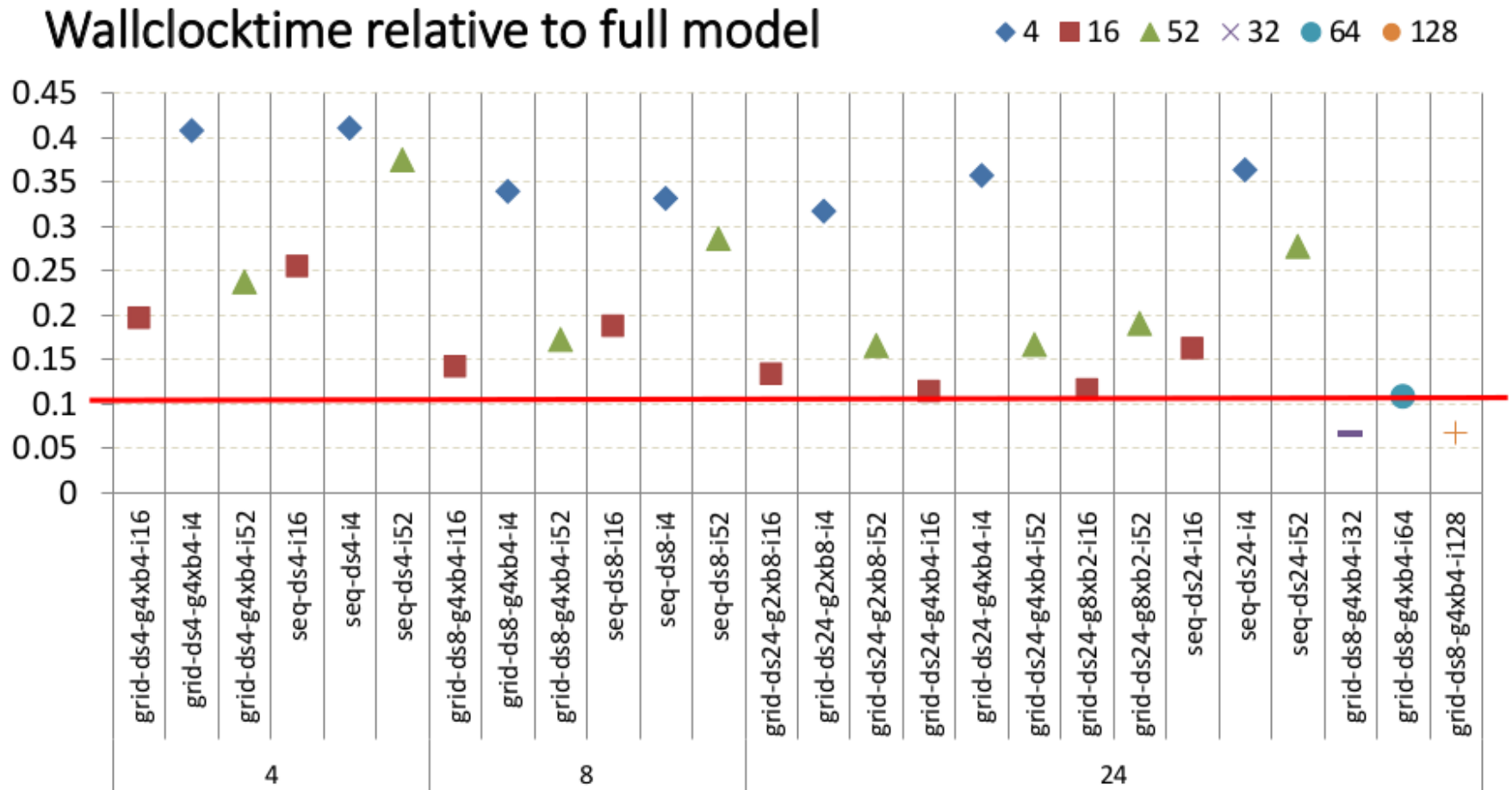
## Accuracy



1 b) Speed-up factor:  $\approx 10$  (2.5)

2 b) Accuracy error mainly  $< 10\%$  (storage:  $\approx 20\%$ )

# Temporal zooming



3) Speed-up factor: >10 reachable, at least >2

# Conclusions

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Which **speed-up** is possible  
using measures that can be  
influenced by „normal“ model  
developers?

# Faktor 10!



- 4 speed-up strategies evaluated
- 2 slightly different models
- Aggregation
  - 1) Speed up  $\approx 5$
  - 2) Accuracy error  $< 10\%^*$
- Temporal zooming
  - 3) Speed up  $\approx 10$

\*except of indicators related to aggregated dimension

# Project BEAM-ME

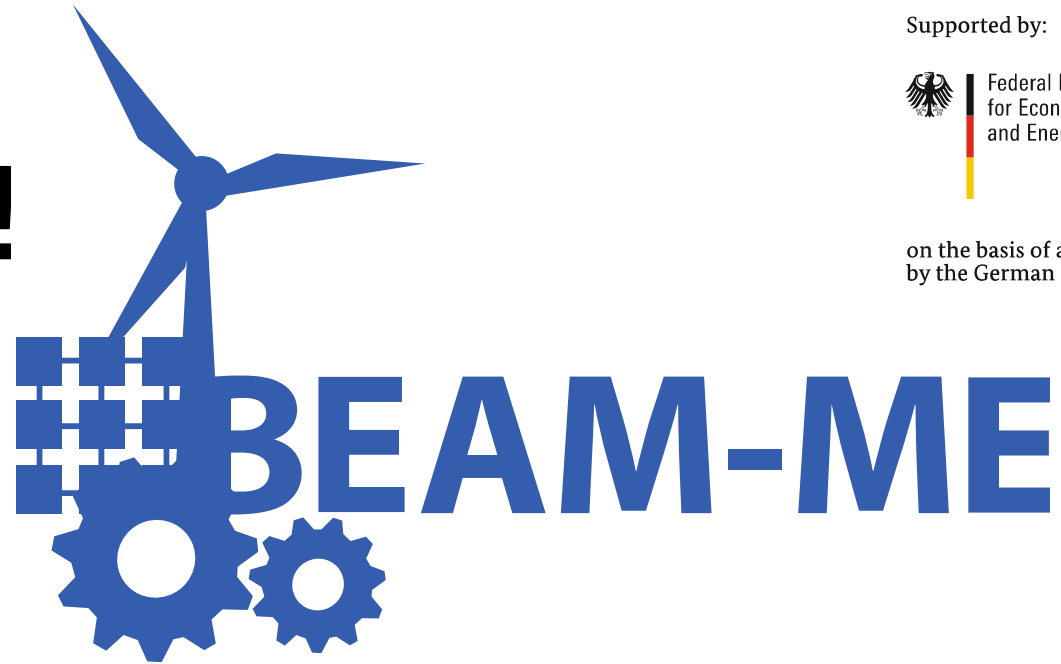
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